

# Lobe, edge, and arc transitivity of graphs of connectivity 1

Jack E. Graver , Mark E. Watkins

*Department of Mathematics, Syracuse University, Syracuse, NY*

Received 27 November 2018, accepted 3 October 2019, published online 9 December 2019

---

## Abstract

We give necessary and sufficient conditions for lobe-transitivity of locally finite and locally countable graphs whose connectivity equals 1. We show further that, given any biconnected graph  $\Lambda$  and a “code” assigned to each orbit of  $\text{Aut}(\Lambda)$ , there exists a unique lobe-transitive graph  $\Gamma$  of connectivity 1 whose lobes are copies of  $\Lambda$  and is consistent with the given code at every vertex of  $\Gamma$ . These results lead to necessary and sufficient conditions for a graph of connectivity 1 to be edge-transitive and to be arc-transitive. Countable graphs of connectivity 1 the action of whose automorphism groups is, respectively, vertex-transitive, primitive, regular, Cayley, and Frobenius had been previously characterized in the literature.

*Keywords:* Lobe, lobe-transitive, edge-transitive, orbit, connectivity.

*Math. Subj. Class.:* 05C25, 05C63, 05C38, 20B27

---

# Reženjska, povezavna in ločna tranzitivnost grafov s povezanostjo 1

Jack E. Graver, Mark E. Watkins

*Department of Mathematics, Syracuse University, Syracuse, NY*

Prejeto 27. novembra 2018, sprejeto 3. oktobra 2019, objavljeno na spletu 9. decembra 2019

---

## Povzetek

Podamo potrebne in zadostne pogoje za reženjsko tranzitivnost lokalno končnih in lokalno števnih grafov, katerih povezanost je enaka 1. Nadalje pokažemo, da za vsak bipovezan graf  $\Lambda$  in "kodo", prirejeno vsaki orbiti grupe  $\text{Aut}(\Lambda)$ , obstaja en sam reženjsko tranzitiven graf  $\Gamma$  s povezanostjo 1, katerega režnji so kopije grafa  $\Lambda$  in je konsistenten z dano kodo v vsakem vozlišču grafa  $\Gamma$ . Ti rezultati vodijo k potrebnim in zadostnim pogojem za to, da je graf s povezanostjo 1 povezavno tranzitiven in ločno tranzitiven. Števniki grafi s povezanostjo 1, za katere je delovanje njihovih grup avtomorfizmov vozliščno tranzitivno, primitivno, regularno, Cayleyjevo ali Frobeniusovo, so bili v literaturi karakterizirani že prej.

*Ključne besede:* Reženj, reženjsko tranzitiven, povezavno tranzitiven, orbita, povezanost.

*Math. Subj. Class.:* 05C25, 05C63, 05C38, 20B27

---